

```

⊢ ∀[P,Q:ℙ]. ((¬P) ∨ (¬Q)) ⇒ (¬(P ∧ Q))
|
BY RepeatFor 2 ((UD THENA Auto))
|
[1]. P: ℙ
[2]. Q: ℙ
⊢ ((¬P) ∨ (¬Q)) ⇒ (¬(P ∧ Q))
|
BY RepeatFor 2 ((D 0 THENA Auto))
|
3. (¬P) ∨ (¬Q)
4. P ∧ Q
⊢ False
|
BY D 4
|
4. P
5. Q
⊢ False
|
BY D 3
| \
| 3. ¬P
| ⊢ False
| |
1 BY (Unfold 'not' 3 THEN D 3)
| | \
| | 3. P
| | 4. Q
| | ⊢ P
| | |
1 2 BY NthHyp 3
|   \
|   3. P
|   4. Q
|   5. False
|   ⊢ False
|   |
1   BY NthHyp 5
|   \
|   3. ¬Q
|   ⊢ False
|
BY (Unfold 'not' 3 THEN D 3).
| \
| 3. P
| 4. Q
| ⊢ Q
| |
1 BY NthHyp 4
|   \
|   3. P
|   4. Q

```

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5. False
⊢ False
|
BY NthHyp 5

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Extract: λf,g. let p,q = g in case f of inl(np) => np p | inr(nq) => nq q
  where f : (¬P) ∨ (¬Q)
        g : P ∧ Q
        p : P
        q : Q
        np : ¬P ≡ (P ⇒ False)
        nq : ¬Q ≡ (Q ⇒ False)

```