

```

⊢ ∀[A,B:ℙ]. {A ∧ B ⇔ ¬((¬A) ∨ (¬B))}
|
BY (D 0 THENA Auto)
| \
| 1. A: ℙ
| ⊢ ∀[B:ℙ]. {A ∧ B ⇔ ¬((¬A) ∨ (¬B))}
| |
1 BY (D 0 THENA Auto)
| | \
| | 2. B: ℙ
| | ⊢ {A ∧ B ⇔ ¬((¬A) ∨ (¬B))}
| | |
1 2 BY RepeatFor 4 ((D 0 THENA Auto))
| | | \
| | | 3. A ∧ B
| | | ⊢ {¬((¬A) ∨ (¬B))}
| | | |
1 2 3 BY (ElimClassical THENA Auto)
| | | |
| | | | ⊢ ¬((¬A) ∨ (¬B))
| | | | |
1 2 3 BY (D 0 THENA Auto)
| | | | |
| | | | 4. (¬A) ∨ (¬B)
| | | | ⊢ False
| | | | |
1 2 3 BY D 3
| | | | |
| | | | 3. A
| | | | 4. B
| | | | 5. (¬A) ∨ (¬B)
| | | | ⊢ False
| | | | |
1 2 3 BY D 5
| | | | \
| | | | 5. ¬A
| | | | ⊢ False
| | | | |
1 2 3 4 BY D 5
| | | | |
| | | | ⊢ A
| | | | |
1 2 3 4 BY Hypothesis
| | | | \
| | | | 5. ¬B
| | | | ⊢ False
| | | | |
1 2 3 BY D 5
| | | | |
| | | | ⊢ B
| | | | |
1 2 3 BY Hypothesis
| | | \
| | | 3. ¬((¬A) ∨ (¬B))
| | | ⊢ {A ∧ B}
| | | |

```

```

1 2  BY RepeatFor 2 (D 0)
| |  | \
| |  | ⊢ {A}
| |  | |
1 2  3 BY (ClassicalContradiction THENA Auto)
| |  | |
| |  | 4. ¬A
| |  | ⊢ {A}
| |  | |
1 2  3 BY D 3
| |  | |
| |  | 3. ¬A
| |  | ⊢ (¬A) ∨ (¬B)
| |  | |
1 2  3 BY (OrLeft THENA Auto)
| |  | |
| |  | ⊢ ¬A
| |  | |
1 2  3 BY Hypothesis
| |  | \
| |  | ⊢ {B}
| |  | |
1 2  BY (ClassicalContradiction THENA Auto)
| |  | |
| |  | 4. ¬B
| |  | ⊢ {B}
| |  | |
1 2  BY D 3
| |  | |
| |  | 3. ¬B
| |  | ⊢ (¬A) ∨ (¬B)
| |  | |
1 2  BY (OrRight THENA Auto)
| |  | |
| |  | ⊢ ¬B
| |  | |
1 2  BY Hypothesis
| |  | \
| |  | 2. B: ℙ
| |  | 3. {x:Unit | A ∧ B ⇔ ¬((¬A) ∨ (¬B))}
| |  | ⊢ Ax ∈ {x:Unit | A ∧ B ⇔ ¬((¬A) ∨ (¬B))}
| |  | |
1  BY Auto
| |  | \
| |  | 1. A: ℙ
| |  | 2. B: ℙ
| |  | 3. {x:Unit | A ∧ B ⇔ ¬((¬A) ∨ (¬B))}
| |  | ⊢ Ax ∈ {x:Unit | A ∧ B ⇔ ¬((¬A) ∨ (¬B))}
| |  | |
| |  | BY Auto

```